

Applied Mathematics for Malting and Brewing Technologists

Technological Calculations, Benchmarks and Correlations for Process Optimization

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